

Fourth Semester MCA Degree Examination, June/July 2018 **Analysis & Design of Algorithms**

Time: 3 hrs. Max. Marks: 100 Note: Answer any FIVE full questions.

Explain worst case, best case and average case efficiencies. (06 Marks)

Solve the following recurrence relation,

A(n) = A(n) + 1 for n > 1 by taking initial condition as A(1) = 0 and $n = 2^{K}$ (04 Marks)

Write algorithms for bubble sort and selection sort and give time complexities for both.

(10 Marks)

- Discuss algorithm design and analysis process. (04 Marks)
 - Explain asymptotic notations.
 - (06 Marks) Analysis time complexity of matrix multiplication. (06 Marks).
 - Define the following terms:
 - (i) Weighted graph
 - (ii) Connected graph.
 - Ordered tree (iii)
 - (iv) Dictionary

(04 Marks)

Illustrate how divide and conquer is applied using quicksort to the following numbers for 3 sorting:

65 70 75 80 85 60 55 50 45

(08 Marks)

Explain time complexity of Mergesort.

- (06 Marks)
- Analysis time complexity of stressen's matrix multiplication.

- (06 Marks)
- Explain general strategies applied in decrease and conquer technique.
- (04 Marks)

Write algorithm for Depth-First search. b.

- (06 Marks)
- Illustrate source-removal algorithm for topological sorting problem.
- (06 Marks)

Write differences between DFS and BFS.

(04 Marks)

Explain about input enhancement.

- Write Harspool's string matching algorithm. Apply this to find the pattern "BARBER" in the text "JIM-SAW ME-IN-A BARBER SHOP". (12 Marks)
- c. Discuss about various types of hashing.

(04 Marks)

Apply dynamic programming technique for the below knapsack problem and find the optimal value of the knapsack.

n = 4 (no. of items) W(capacity) = 5

(10 Marks)

Į	Item	1	2	3	4
	Weight	2	1	3	2
	Profit	12	10	20	15

Write Floyd's algorithm.

(05 Marks)

Write an algorithm for computing the binomial coefficient C(n, K) using dynamic programming. (05 Marks)

7 a. Write Prim algorithm and apply the same to find minimum cost spanning tree for the following graph. (10 Marks)

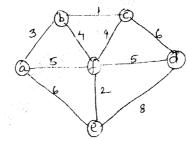


Fig. Q7 (a)

b. Apply Dijkstra algorithm to the following graph:

(05 Marks)

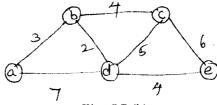


Fig. Q7 (b)

c. Apply Branch-bound technique for knapsack problem by taking following values: n = 4, m = 10 (weight of knapsack)

$$(P_1, P_2, P_3, P_4) = (40,42,25,12)$$

$$(W_1, W_2, W_3, W_4) = (4,7,5,3)$$

(05 Marks)

- 8 a. Draw Decision trees for 3 elements selection sort and binary search in a four element array (06 Marks
 - b. Write algorithm for Back tracking and draw state-space tree for four queen's problem using back tracking.

 (08 Mark)
 - c. Explain about P, NP and NP-complete.

(06 Mark